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Scheduling Examples for Constraint Acquisition

Helmut Simonis
Insight SFI Centre for Data Analytics
School of Computer Science and Information Technology
University College Cork, Cork, Ireland



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Overview

- Why scheduling is a good field for Constraint Acquisition (CA)
- Present what scheduling problems looks like
- From simple to complex
- Give links to data in literature
- Show some realistic examples
- Focus on data, not algorithms

Why Scheduling?

- This is the most successful application area for Constraint Programming (CP)
- Huge variety of different problem types and sub-types
- Often involves optimization of some objective(s)
- CP works best when there are many side constraints
 - Easy to add to a model
- There is a lot of literature
- Scheduling is important for many users

Challenges

- Nearly always instances of different sizes
- Underlying problem is constantly evolving
 - New/deleted products, processes, machines
 - You need snapshot of relevant background data to reproduce results
- Nobody is interested in resolving previously solved instances
 - Unless you find better objective value
- There is rarely more than one solution kept for each instance
- Typically no non-solutions are produced and/or stored
- You may have different plans based on compromises between objectives/stakeholders

Challenges (II)

- New instances are constantly added (every day)
 - We need to generate solutions for these unseen instances
- Big difference between planned schedule and actual, observed schedule
 - Machine break-downs
 - Quality issues, rework
 - Rush-orders, cancellations
 - Impact of (lack of) component stock
- Don't do as I do, do as I say
 - You don't want to learn the bad ways of fire-fighting
 - Hope that the original plan is stored, as well as the actual production data

Existing Literature

- Methods to Learn Abstract Scheduling Models. Carchrae, Beck, Freuder. CP 2005. [9]
 - Suggests backdoor based approach to project scheduling
- Learning Scheduling Models from Event Data. Senderovich, Booth, Beck. ICAPS 2019. [40]
 - Learning models from traces of execution of actual schedules
- Guided Bottom-Up Interactive Constraint Acquisition. Tsouros, Berden, Guns. CP 2023. [42]
 - Example of smallish job-shop problem
- Boolean-Arithmetic Equations: Acquisition and Uses. Gindullin, Beldiceanu, Cheukam-Ngouonou, Douence, Quimper. CPAIOR 2023. [18]
 - Learning formulas from tables

My Interest

- "Passive" Constraint Acquisition
 - Learn from positive (negative) examples
 - Few (one) solutions per instances, many instances
- Search for transferable model
 - Learn model from samples, apply to unseen instances
- Deal with large number of hidden variables
 - Stored results only show actionable decisions
- No membership queries for humans
 - Ask more meaningful questions: Can you interrupt execution of a task on this machine?
 - Automated oracles can only answer full queries

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Examples from Books on CP

- Can we acquire the models of scheduling problems in books on CP?
- Which books? There are books?

Books on CP

| Author | Title | Year | Pages | Language | CP System | Exercises |
|------------------------------|--|------|-------|----------|---------------------------|-----------|
| P Van Hentenryck | Constraint satisfaction in logic programming[20] | 1989 | 224 | English | CHIP[12] | - |
| F. Fages | Programmation logique par contraintes[13] | 1996 | 192 | French | GNU Prolog | yes |
| K. Marriott, P. Stuckey | Programming with Constraints[32] | 1998 | 467 | English | CLP(R)[27] | yes |
| P Van Hentenryck | The OPL Optimization Programming Language[21] | 1999 | 254 | English | OPL[22] | ??? |
| J. Hooker | Logic-Based Methods for Optimization[24] | 2000 | 495 | English | - | no |
| K. Apt | Principles of Constraint Programming[2] | 2003 | 407 | English | - | yes |
| R. Dechter | Constraint processing[11] | 2003 | 481 | English | - | ??? |
| T. Frühwirth, S. Abdennadher | Essentials of constraint programming[14] | 2003 | 156 | English | CHR | no |
| K. Apt, M. Wallace | Constraint Logic Programming using ECLiPSe [3] | 2007 | 329 | English | ECLiPSe[39] | yes |
| J. Hooker | Integrated Methods for Optimization[25] | 2007 | 486 | English | - | yes |
| P. Hofstedt, A. Wolf | Einführung in die Constraint-Programmierung[23] | 2007 | 388 | German | TURTLE[19] firstcs[44] | yes |

Books on CP (II)

| Author | Title | Year | Pages | Language | CP System | Exercises |
|---|---|------|-------|----------|-------------------------------------|-----------|
| D. Poole, A. Mackworth | Artificial Intelligence - Foundations of Computational Agents[35] | 2010 | 900 | English | - | yes |
| C. Lecoutre | Constraint Networks: Targeting Simplicity for Techniques and Algorithms[30] | 2013 | 320 | English | ??? | ??? |
| A. Niederlinski | A Gentle Guide to Constraint Logic Programming via ECLiPSe[34] | 2014 | 509 | English | ECLiPSe[39] | yes |
| E. Tsang | Foundations of Constraint Satisfaction: The Classic Text[41] | 2014 | 444 | English | ??? | ??? |
| N. Zhou, H. Kjellerstrand, J. Fruhman | Constraint Solving and Planning with Picat[46] | 2015 | 140 | English | Picat[45] | yes |
| E. Bourreau, M. Gondran, P. Lacomme, M. Vinot | De la programmation linéaire à la programmation par contraintes[7] | 2019 | 348 | French | Gusek CPLEX GLPK Choco[37] | no |
| E. Bourreau, M. Gondran, P. Lacomme, M. Vinot | Programmation par Contraintes[8] | 2020 | 232 | French | Choco[37] | no |
| S. Russell, P. Norvig | Artificial Intelligence: A Modern Approach (4th Edition)[38] | 2020 | 1115 | English | - | no |
| M. Wallace | Building Decision Support Systems - using MiniZinc[43] | 2020 | 224 | English | MiniZinc[33] | yes |

Source: Workshop on Teaching Constraint Programming, Santanam, Simonis, 2023

- Tejas and myself are working on overview paper based on workshop
- Exists in draft form, if you are interested
- If you are teaching a CP course, please fill in
 - <https://forms.gle/v54HUsbSXcyHmfME9>
 - or contact us!

Constraint Programming Education Survey

Hello! We kindly ask for 5 minutes of your time for the following survey on CP courses. This information will be used for discussion at the WTCP 2023 workshop in Toronto, as well as for general understanding on educational practices within the CP community.

helmut.simonis.eerk@gmail.com [Switch account](#)

* indicates required question

Email *

Your email

Does your institution offer a CP course or a course that covers some content around CP, SAT, or similar?

Yes

No

If no, what are the barriers or reasons?

Your answer

If your institution offers such a course, is there more than one course that covers some aspect of this topic?

Yes

No

If you answered yes to the first question, who is the audience?

Undergraduates

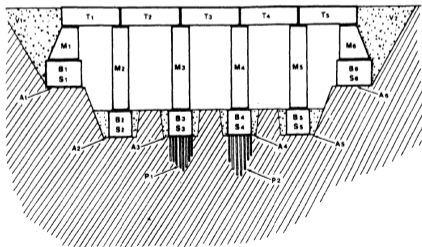
Graduate Students

Some Example Scheduling Problems

- Importance of data to acquire problem
- Constraint structure given as part of data, or implicit as part of problem structure
- Very often: data hardcoded in program
 - It saves space...
 - We should not teach this

Bridge Scheduling Problem (Van Hentenryck 1989 [20])

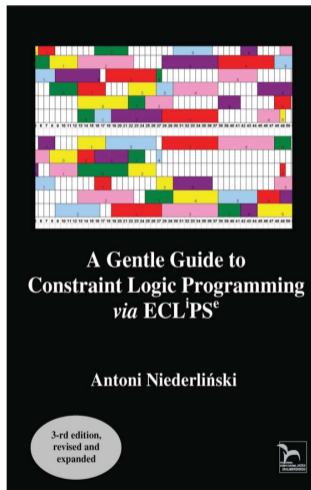
- First scheduling problem with CHIP
- Based on PhD thesis of Bartusch
- Disjunctive Scheduling (RCPSP)
- Different types of temporal relations
- Minimize makespan



| N | Name | description | duration | resource |
|----|------|------------------------------------|----------|----------------|
| 1 | PA | beginning of project | 0 | - |
| 2 | A1 | excavation (abutment 1) | 4 | excavator |
| 3 | A2 | excavation (pillar 1) | 2 | excavator |
| 4 | A3 | excavation (pillar 2) | 2 | excavator |
| 5 | A4 | excavation (pillar 3) | 2 | excavator |
| 6 | A5 | excavation (pillar 4) | 2 | excavator |
| 7 | A6 | excavation (abutment 2) | 5 | excavator |
| 8 | P1 | foundation piles 2 | 20 | pile-driver |
| 9 | P2 | foundation piles 3 | 13 | pile-driver |
| 10 | UE | erection of temporary housing | 10 | - |
| 11 | S1 | formwork (abutment 1) | 8 | carpentry |
| 12 | S2 | formwork (pillar 1) | 4 | carpentry |
| 13 | S3 | formwork (pillar 2) | 4 | carpentry |
| 14 | S4 | formwork (pillar 3) | 4 | carpentry |
| 15 | S5 | formwork (pillar 4) | 4 | carpentry |
| 16 | S6 | formwork (abutment 2) | 10 | carpentry |
| 17 | B1 | concrete foundation (abutment 1) | 1 | concrete-mixer |
| 18 | B2 | concrete foundation (pillar 1) | 1 | concrete-mixer |
| 19 | B3 | concrete foundation (pillar 2) | 1 | concrete-mixer |
| 20 | B4 | concrete foundation (pillar 3) | 1 | concrete-mixer |
| 21 | B5 | concrete foundation (pillar 4) | 1 | concrete-mixer |
| 22 | B6 | concrete foundation (abutment 2) | 1 | concrete-mixer |
| 23 | AB1 | concrete setting time (abutment 1) | 1 | - |
| 24 | AB2 | concrete setting time (pillar 1) | 1 | - |
| 25 | AB3 | concrete setting time (pillar 2) | 1 | - |
| 26 | AB4 | concrete setting time (pillar 3) | 1 | - |
| 27 | AB5 | concrete setting time (pillar 4) | 1 | - |
| 28 | AB6 | concrete setting time (abutment 2) | 1 | - |
| 29 | M1 | masonry work (abutment 1) | 16 | bricklaying |
| 30 | M2 | masonry work (pillar 1) | 8 | bricklaying |
| 31 | M3 | masonry work (pillar 2) | 8 | bricklaying |
| 32 | M4 | masonry work (pillar 3) | 8 | bricklaying |
| 33 | M5 | masonry work (pillar 4) | 8 | bricklaying |
| 34 | M6 | masonry work (abutment 2) | 20 | bricklaying |
| 35 | L | delivery of the preformed bearers | 2 | crane |
| 36 | T1 | positioning (preformed bearer 1) | 12 | crane |
| 37 | T2 | positioning (preformed bearer 2) | 12 | crane |
| 38 | T3 | positioning (preformed bearer 3) | 12 | crane |
| 39 | T4 | positioning (preformed bearer 4) | 12 | crane |
| 40 | T5 | positioning (preformed bearer 5) | 12 | crane |
| 41 | UA | removal of the temporary housing | 10 | - |
| 42 | V1 | filling 1 | 15 | caterpillar |
| 43 | V2 | filling 2 | 10 | caterpillar |
| 44 | K1 | point 1 of cost function | 0 | - |
| 45 | K2 | point 2 of cost function | 0 | - |
| 46 | DE | end of project | 0 | - |

A Gentle Guide to Constraint Logic Programming (Niederlinski 2014 [34])

- Discusses many scheduling examples
- Most are open-coded, no separation of program and data
- ECLiPSe code given
- Result visualizations given



Ship Loading Example

```

/*9*/  LS  :: 1..400,
/*10*/ LD  :: 1..40,
/*11*/ LR  :: 1..12,
/*12*/ End  :: 1..400,
/*13*/ Limit :: 1..12,

/*14*/ cumulative(LS,LD,[R1,R2,R3,R4,R5,R6,R7],R8,R9,R10,R11,
    R12,R13,R14,R15,R16,R17,R18,R19,R20,R21,R22,
    R23,R24,R25,R26,R27,R28,R29,R30,R31,R32,R33,R34],
    LF,Limit),

/*15*/ S1 + D1 #=< S2,
/*16*/ S1 + D1 #=< S4,
/*17*/ S2 + D2 #=< S3,
/*18*/ S3 + D3 #=< S5,
/*19*/ S3 + D3 #=< S7,
/*20*/ S4 + D4 #=< S5,
/*21*/ S5 + D5 #=< S6,
/*22*/ S6 + D6 #=< S8,
/*23*/ S7 + D7 #=< S8,
/*24*/ S8 + D8 #=< S9,
/*25*/ S9 + D9 #=< S10,
/*26*/ S9 + D9 #=< S14,
/*27*/ S10 + D10 #=< S11,
/*28*/ S10 + D10 #=< S12,
/*29*/ S11 + D11 #=< S13,
/*30*/ S12 + D12 #=< S13,
/*31*/ S13 + D13 #=< S15,
/*32*/ S13 + D13 #=< S16,
/*33*/ S14 + D14 #=< S15,
/*34*/ S15 + D15 #=< S18,
/*35*/ S16 + D16 #=< S17,
/*36*/ S17 + D17 #=< S18,
/*37*/ S18 + D18 #=< S19,
/*38*/ S18 + D18 #=< S20,

```

| Task | Man-hours | Next task |
|------|-----------|-------------|
| 1 | 12 | 2, 4 |
| 2 | 16 | 3 |
| 3 | 12 | 5, 7 |
| 4 | 24 | 5 |
| 5 | 25 | 6 |
| 6 | 10 | 8 |
| 7 | 12 | 8 |
| 8 | 12 | 9 |
| 9 | 12 | 10, 14 |
| 10 | 16 | 11, 12 |
| 11 | 12 | 13 |
| 12 | 10 | 13 |
| 13 | 4 | 15,16 |
| 14 | 15 | 15 |
| 15 | 6 | 18 |
| 16 | 9 | 17 |
| 17 | 12 | 18 |
| 18 | 14 | 19, 20, 21 |
| 19 | 4 | 23 |
| 20 | 4 | 23 |
| 21 | 4 | 22 |
| 22 | 8 | 23 |
| 23 | 28 | 24 |
| 24 | 40 | 25 |
| 25 | 16 | 26,30,31,32 |
| 26 | 3 | 27 |
| 27 | 3 | 28 |
| 28 | 12 | 29 |
| 29 | 8 | end |
| 30 | 9 | 28 |
| 31 | 6 | 28 |
| 32 | 3 | 28 |
| 33 | 6 | 34 |
| 34 | 6 | end |

Job-Shop (Wallace, 2020 [43])

```
int: n_machines;
int: n_jobs;
int: n_tasks = n_machines;
set of int: jobs = 1..n_jobs;
set of int: tasks = 1..n_tasks;
set of int: machines = 1..n_machines ;
array [jobs, tasks] of machines: jt_machine;
array [jobs, tasks] of int: jt_duration;
int: max_end = 1050 ;

array [jobs, tasks] of var 0.. max_end: jt_start;
var 0..max_end: t_end ;

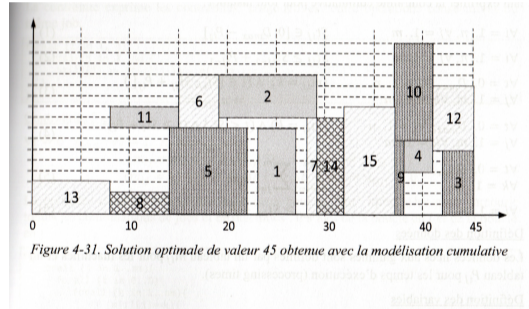
constraint
forall ( j in jobs, k in 1..(n_tasks - 1) ) (
    jt_start[j, k] + jt_duration[j, k] <=
        jt_start[j, k + 1]
);
include "disjunctive.mzn" ;
constraint
forall(m in machines)
    (disjunctive(
        [jt_start[j,t]|j in jobs,t in tasks where jt_machine[j,t]=m],
        [jt_duration[j,t]|j in jobs, t in tasks where jt_machine[j,t]=m]
    )
);

solve minimize t_end ;
```

```
n_jobs = 10;
n_machines = 10;
jt_machine = array2d(jobs, tasks,
[ 0, 1, 2, 3, 4, 5, 6, 7, 8, 9,
0, 2, 4, 9, 3, 3, 1, 6, 5, 7, 8,
1, 0, 3, 2, 8, 5, 7, 6, 9, 4,
1, 2, 0, 4, 6, 8, 7, 3, 9, 5,
2, 0, 1, 5, 3, 4, 8, 7, 9, 6,
2, 1, 5, 3, 8, 9, 0, 6, 4, 7,
1, 0, 3, 2, 6, 5, 9, 8, 7, 4,
2, 0, 1, 5, 4, 6, 8, 9, 7, 3,
0, 1, 3, 5, 2, 9, 6, 7, 4, 8,
1, 0, 2, 6, 8, 9, 5, 3, 4, 7 ]);
jt_duration = array2d(jobs, tasks, [
29, 78, 9, 36, 49, 11, 62, 56, 44, 21,
43, 90, 75, 11, 69, 28, 46, 46, 72, 30,
91, 85, 39, 74, 90, 10, 12, 89, 45, 33,
81, 95, 71, 99, 9, 52, 85, 98, 22, 43,
14, 6, 22, 61, 26, 69, 21, 49, 72, 53,
84, 2, 52, 95, 48, 72, 47, 65, 6, 25,
46, 37, 61, 13, 32, 21, 32, 89, 30, 55,
31, 86, 46, 74, 32, 88, 19, 48, 36, 79,
76, 69, 76, 51, 85, 11, 40, 89, 26, 74,
85, 13, 61, 7, 64, 76, 47, 52, 90, 45
]);
```

Resource-Constrained Project Scheduling Problem (RCPSP) (Bourreau et al., 2019 [7])

- RCPSP with different approaches
- Different solvers, Choco-Solver, OPL Studio
- Complete Java projects
- Focus on modelling alternatives, performance
- Partial search (LDS)
- Also considers job-shop



Common Points

- A good number of scheduling problems are presented
- Often not in a form that allows Constraint Acquisition to work
- Needs a lot of work to present data and solutions in machine readable form
- Resulting models are easy for tools to find, even with single (few) positive examples

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Motivation

- More and more papers attach data
- But, every paper uses different format
- CA ideally should be able to deal with these
- Broad basis for requirements analysis
- Most papers do not make it easy to understand data

Methodology

- Use DBLP as primary source
- Extract relevant meta-data
- Text analysis of pdf to find shared concepts
- Manual extraction of some features

Existing Literature Surveys

- Optimal methods for resource allocation and scheduling: a cross-disciplinary survey. Lombardi, Milano. 2012 [31].
 - Compares CP, MIP and hybrid methods
 - Gives examples of models and solution methods
 - From 2012, a lot of progress since then
- Applications of constraint programming in production scheduling problems: A descriptive bibliometric analysis. Prata, Abreu, and Nagano. 2024 [36].
 - Deeply flawed paper: data, methodology and analysis
 - Only focuses on flow/job/open shop

Literature Survey - Recent Articles

Table 3: Articles from bibtex

| Key | Authors | Title | LC | Cite | Year | Journal | Pages |
|-------------------------------|---|---|----|-------|------|---|-------|
| PrataAN23 PrataAN23 | Bruno A. Prata, Levi R. Abreu, Marcelo S. Nagano | Applications of constraint programming in production scheduling problems: A descriptive bibliometric analysis | | [312] | 2024 | Results in Control and Optimization | 1 |
| abs-2402-00459 abs-2402-00459 | S. Nguyen, Dhananjay R. Thiruvady, Y. Sun, M. Zhang | Genetic-based Constraint Programming for Resource Constrained Job Scheduling | | [279] | 2024 | CoRR | null |
| AbreuNP23 AbreuNP23 | Levi Ribeiro de Abreu, Marcelo Seido Nagano, Bruno A. Prata | A new two-stage constraint programming approach for open shop scheduling problem with machine blocking | NO | [90] | 2023 | Int. J. Prod. Res. | 20 |
| AkramNHRS23 AkramNHRS23 | Bilal Omar Akram, Nor Kamariah Noordin, F. Hashim, Mohd Fadlee A. Rasid, Mustafa Ismael Salman, Abdulrahman M. Abdulghani | Joint Scheduling and Routing Optimization for Deterministic Hybrid Traffic in Time-Sensitive Networks Using Constraint Programming | | [7] | 2023 | IEEE Access | 16 |
| Caballero23 Caballero23 | Jordi Coll Caballero | Scheduling through logic-based tools | | [71] | 2023 | Constraints An Int. J. | 1 |
| GurPAE23 GurPAE23 | S. Gür, M. Pinarbasi, Haci Mehmet Alakas, T. Eren | Operating room scheduling with surgical team: a new approach with constraint programming and goal programming | | [157] | 2023 | Central Eur. J. Oper. Res. | 25 |
| IsikYA23 IsikYA23 | Eyüp Ensar Isik, Seyda Topaloglu Yildiz, Özge Satir Akpunar | Constraint programming models for the hybrid flow shop scheduling problem and its extensions | | [186] | 2023 | Soft Comput. | 28 |
| LacknerMMWW23 LacknerMMWW23 | M. Lackner, C. Mrkvicka, N. Musliu, D. Walkiewicz, F. Winter | Exact methods for the Oven Scheduling Problem | | [224] | 2023 | Constraints An Int. J. | 42 |
| MontemanniD23 MontemanniD23 | R. Montemanni, M. Dell'Amico | Solving the Parallel Drone Scheduling Traveling Salesman Problem via Constraint Programming | | [268] | 2023 | Algorithms | 1 |
| MontemanniD23a MontemanniD23a | R. Montemanni, M. Dell'Amico | Constraint programming models for the parallel drone scheduling vehicle routing problem | | [267] | 2023 | EURO J. Comput. Optim. | 1 |
| ShaikhK23 ShaikhK23 | Aftab Ahmed Shaikh, Abdullah Ayub Khan | Management of electronic ledger: a constraint programming approach for solving curricula scheduling problems | NO | [336] | 2023 | Int. J. Electron. Secur. Digit. Forensics | 12 |
| YuraszckMCCR23 YuraszckMCCR23 | F. Yuraszck, E. Montero, D. Canut-de-Bon, N. Cuneo, M. Rojfel | A Constraint Programming Formulation of the Multi-Mode Resource-Constrained Project Scheduling Problem for the Flexible Job Shop Scheduling Problem | | [406] | 2023 | IEEE Access | 11 |
| abs-2305-19888 abs-2305-19888 | V. Heinz, A. Novák, M. Vlk, Z. Hanzálek | Constraint Programming and Constructive Heuristics for Parallel Machine Scheduling with Sequence-Dependent Setups and Common Servers | | [170] | 2023 | CoRR | null |
| abs-2306-05747 abs-2306-05747 | P. Tassel, M. Gebser, K. Schekotihin | An End-to-End Reinforcement Learning Approach for Job-Shop Scheduling Problems Based on Constraint Programming | | [356] | 2023 | CoRR | null |
| abs-2312-13682 abs-2312-13682 | G. Perez, G. Glorian, W. Suijlen, A. Lallouet | A Constraint Programming Model for Scheduling the Unloading of Trains in Ports: Extended | | [300] | 2023 | CoRR | null |
| AbreuN22 AbreuN22 | Levi Ribeiro de Abreu, Marcelo Seido Nagano | A new hybridization of adaptive large neighborhood search with constraint programming for open shop scheduling with sequence-dependent setup times | | [89] | 2022 | Comput. Ind. Eng. | 1 |
| BourreauGGLT22 BourreauGGLT22 | E. Bourreau, T. Garaix, M. Gondran, P. Lacomme, N. Tchernev | A constraint-programming based decomposition method for the Generalised Workforce Scheduling and Routing Problem (GWSRP) | NO | [68] | 2022 | Int. J. Prod. Res. | 19 |
| CampeauG22 CampeauG22 | L. Campeau, M. Gamache | Short- and medium-term optimization of underground mine planning using constraint programming | | [72] | 2022 | Constraints An Int. J. | 18 |
| FetgoD22 FetgoD22 | Sévérine Betmbe Fetgo, Clémentin Tayou Djamégni | Horizontally Elastic Edge-Finder Algorithm for Cumulative Resource Constraint Revisited | | [116] | 2022 | Oper. Res. Forum | null |
| HeinzNVH22 HeinzNVH22 | V. Heinz, A. Novák, M. Vlk, Z. Hanzálek | Constraint Programming and constructive heuristics for parallel machine scheduling with sequence-dependent setups and common servers | CP | [169] | 2022 | Comput. Ind. Eng. | 1 |



Literature Survey - Extracted Concepts

Table 7: Keywords by Work and Domains

| Work | Concepts | Classification | Constraints | ProgLanguages | CPSystems | Areas | Industries | Benchmarks | Algorithm |
|------------------------------------|---|--|---|---------------|---|--------------------------------------|--|---|---------------------|
| PrataAN23 [312] | scheduling, order, job, task, activity, resource, machine, precedence, preempt, sequence dependent setup, inventory, make span, completion time, flow time, lateness, tardiness, earliness, flow shop, job shop, open shop, release date, due date, setup time, distributed, re scheduling, batch process | single machine, parallel machine, Open Shop Scheduling Problem | cumulative, circuit | | CHIP | aircraft, robot, energy price, dairy | manufacturing industry | benchmark, real world, real life, http:// , https:// | time tabling |
| abs-2402-00459 [279] | scheduling, order, job, task, resource, machine, precedence, completion time, tardiness, earliness, job shop, due date, multi agent | single machine | cumulative, disjunctive, bin packing | | or tools | | mining industry | benchmark, generated instance, instance generator, real world, http:// , https:// , github | |
| AbreuNP23 [90] AkramNHRSA23 [7] | scheduling, order, task, resource, machine, preempt, completion time, distributed | | bin packing | python | or tools | agriculture, medical | | benchmark, https:// | |
| Caballero23 [71] | scheduling, resource | RCPSP | | | | | | http:// , https:// | |
| GurPAE23 [157] | scheduling, order, resource, machine, inventory, distributed, re scheduling | | cumulative | | cplex | physician, nurse, patient, COVID | | real life, https:// | |
| IsikYA23 [186] | scheduling, order, job, task, resource, machine, precedence, preempt, sequence dependent setup, transportation, make span, cmax, completion time, tardiness, earliness, flow shop, job shop, release date, due date, setup time, distributed, batch process | single machine, parallel machine | cumulative, circuit, nooverlap, endbeforestart | | cplex, OPL | medical, robot | steel industry | benchmark, generated instance, real world, real life, http:// , https:// | energetic reasoning |
| LacknerMMWW23 [224] | scheduling, order, job, task, machine, make span, lateness, tardiness, earliness, job shop, release date, due date, setup time, batch process | single machine, parallel machine, OSP | alternative constraint, cumulative, disjunctive, nooverlap, endbeforestart, bin packing | | cplex, gurobi, or tools, OPL, cpo, chuffed, mini zinc | semiconductor, oven scheduling | electronics industry, manufacturing industry, steel industry | benchmark, instance generator, random instance, real life, industrial partner, http:// , https:// , zenodo | time tabling |
| MontemanniD23 [268] | scheduling, order, task, resource, machine, distributed | | circuit | python | gurobi, or tools | robot | | benchmark, supplementary material, https:// | |
| MontemanniD23a [267] | scheduling, order, task, transportation, completion time | | circuit | python | or tools | | | benchmark, http:// , https:// | |

Literature Survey - Supplementary Materials

Table 4: Article Properties

| Key | Title | CP System | Data Avail | Sol Avail | Code Avail | Based On | Classification | Constraints |
|-------------------------------|---|------------------|-------------|-----------|------------|------------|----------------------|--|
| PrataAN23 PrataAN23 | Applications of constraint programming in production scheduling problems: A descriptive bibliometric analysis | - | - | - | - | - | survey | - |
| abs-2402-00459 abs-2402-00459 | Genetic-based Constraint Programming for Resource Constrained Job Scheduling | OR-Tools | y | - | n | - | RCJS | cumulatives |
| AbreuNP23 AbreuNP23 | A new two-stage constraint programming approach for open shop scheduling problem with machine blocking | ? | ? | - | ? | ? | ? | ? |
| AkramNHRSA23 AkramNHRSA23 | Joint Scheduling and Routing Optimization for Deterministic Hybrid Traffic in Time-Sensitive Networks Using Constraint Programming | OR-Tools | n | - | n | - | TSN | - |
| Caballero23 Caballero23 | Scheduling through logic-based tools | SAT | - | - | - | PhD Thesis | RCPSP | - |
| GurPAE23 GurPAE23 | Operating room scheduling with surgical team: a new approach with constraint programming and goal programming | Cplex | n | - | n | - | - | - |
| IsikYA23 IsikYA23 | Constraint programming models for the hybrid flow shop scheduling problem and its extensions | OPL CP Opt | y | - | y | - | HFSP | alternative endBeforeStart noOverlap cumulative alternative noOverlap |
| LacknerMMWW23 LacknerMMWW23 | Exact methods for the Oven Scheduling Problem | MiniZinc OPL | DZN JSON | - | y | [223] | OSP | alternative noOverlap forbidExtent circuit |
| MontemanniD23 MontemanniD23 | Solving the Parallel Drone Scheduling Traveling Salesman Problem via Constraint Programming | OR-Tools | ref | y | n | - | PDSTSP | circuit multipleCircuit |
| MontemanniD23a MontemanniD23a | Constraint programming models for the parallel drone scheduling vehicle routing problem | OR-Tools | ref | - | n | - | PDSTSP | ? |
| ShaikhK23 ShaikhK23 | Management of electronic ledger: a constraint programming approach for solving curricula scheduling problems | ? | ? | - | ? | ? | ? | ? |
| YuraszckMCCR23 YuraszckMCCR23 | A Constraint Programming Formulation of the Multi-Mode Resource-Constrained Project Scheduling Problem for the Flexible Job Shop Scheduling Problem | CP Opt | ref | - | n | - | FJSSP | alternative endBeforeStart cumulative alternative noOverlap cumulative noOverlap |
| abs-2305-19888 abs-2305-19888 | Constraint Programming and Constructive Heuristics for Parallel Machine Scheduling with Sequence-Dependent Setups and Common Servers | CP Opt Gurobi | y | y | n | - | $P seq, ser C_{max}$ | alternative noOverlap cumulative noOverlap |
| abs-2306-05747 abs-2306-05747 | An End-to-End Reinforcement Learning Approach for Job-Shop Scheduling Problems Based on Constraint Programming | custom Choco | ref | - | n | - | JSSP | noOverlap |
| abs-2312-13682 abs-2312-13682 | A Constraint Programming Model for Scheduling the Unloading of Trains in Ports: Extended | custom | n | - | n | - | SUTP | table disjunctive |
| AbreuN22 AbreuN22 | A new hybridization of adaptive large neighborhood search with constraint programming for open shop scheduling with sequence-dependent setup times | Cplex CP Opt | y | - | n | - | OSSPST | noOverlap |
| BourreauGGLT22 BourreauGGLT22 | A constraint-programming based decomposition method for the Generalised Workforce Scheduling and Routing Problem (GWSRP) | - | - | - | - | - | - | - |
| CampeauG22 CampeauG22 | Short- and medium-term optimization of underground mine planning using constraint programming | CP Opt | ref | - | n | - | - | pulse alwaysIn endBeforeStart noOverlap |
| FetgoD22 FetgoD22 | Horizontally Elastic Edge-Finder Algorithm for Curative Resource Constraint Revisited | - | - | - | - | - | - | - |
| HeinzNVH22 HeinzNVH22 | Constraint Programming and constructive heuristics for | - | - | - | - | - | - | - |



Literature Survey - The same for Papers

Table 2: Paper Properties

| Key | Title | CP System | Data Avail | Sol Avail | Code Avail | Based On | Classification | Constraints |
|--|---|--|----------------------|-----------|------------|----------|--------------------------|--|
| AalianPG23 AalianPC23 | Optimization of Short-Term Underground Mine Planning Using Constraint Programming | CP Opt | n | | n | | | ? |
| Bit-Monnot23 Monnot23 | Enhancing Hybrid CP-SAT Search for Disjunctive Scheduling | ARIES CP Opt OR-Tools Mistral OR-Tools | y | | y | - | JSSP OSSP | - |
| EfthymiouY23 EfthymiouY23 | Predicting the Optimal Period for Cyclic Hoist Scheduling Problems | Mistral OR-Tools | n | | n | - | CHSP | - |
| JuvinHHL23 HHL23 | An Efficient Constraint Programming Approach to Pre-emptive Job Shop Scheduling | CP Opt Mistral | ref | | y | | PJSSP | endBeforeStart span |
| JuvinHL23 JuvinHL23 | Constraint Programming for the Robust Two-Machine Flow-Shop Scheduling Problem with Budgeted Uncertainty | CP Opt Cplex | ref | | n | - | Perm FSSP | noOverlap endBeforeStart noOverlap sameSequence cumulative |
| KameugneFND23 KameugneFND23 | Horizontally Elastic Edge Finder Rule for Cumulative Constraint Based on Slack and Density | ? | BL PSPlib | | n | - | RCPSPs | |
| KimCMLLP23 KimCM-LLP23 | Iterated Greedy Constraint Programming for Scheduling Steelmaking Continuous Casting | Gurobi OR-Tools | y | | n | - | SCC | alternative noOverlap |
| Mehdizadeh-Somarin23 Mehdizadeh-Somarin23 | A Constraint Programming Model for a Reconfigurable Job Shop Scheduling Problem with Machine Availability | CP Opt | n | | n | - | JSSP RMS | alternative endBeforeStart noOverlap |
| PerezGSL23 PerezGSL23 | A Constraint Programming Model for Scheduling the Unloading of Trains in Ports | custom | n | | n | - | SUTP | table disjunctive |
| PovedaAA23 PovedaAA23 | Partially Preemptive Multi Skill/Mode Resource-Constrained Project Scheduling with Generalized Precedence Relations and Calendars | CP Opt MiniZinc Chuffed | y | | y | | PP-MS-MMRCPSP/max-cal | |
| Squillacipr23 Squillacipr23 | Scheduling Complex Observation Requests for a Constellation of Satellites: Large Neighborhood Search Approaches | Cplex Studio | y | | n | - | EOSP | ? |
| TardivoDFMP23 TardivoDFMP23 | Constraint Propagation on GPU: A Case Study for the Cumulative Constraint | MiniCPP MiniZinc | PSPLib BL Pack | | y | - | RCPSP | cumulative |
| TasselGS23 TasselGS23 | An End-to-End Reinforcement Learning Approach for Job-Shop Scheduling Problems Based on Constraint Programming | custom Choco | ref | | y | - | JSSP | noOverlap |
| WangB23 WangB23 | Dynamic All-Different and Maximal Cliques Constraints for Fixed Job Scheduling | FaCiLe | (y) | | n | [390] | FJS | - |
| YuraszeckMC23 YuraszeckMC23 | A competitive constraint programming approach for the group shop scheduling problem | CP Opt | ref | | n | - | GSSP | noOverlap endBeforeStart |
| ArmstrongGOS22 strongGOS22 | A Two-Phase Hybrid Approach for the Hybrid Flexible Flowshop with Transportation Times | CP Opt | (y) | | - | [13] | HFFM tt C _{max} | endBeforeStart alternative cumulative noOverlap cumulative |
| BoudreaultSLQ22 BoudreaultSLQ22 | A Constraint Programming Approach to Ship Refit Project Scheduling | MiniZinc Chuffed | | | y | - | RCPSP | cumulative |
| GeitzGSSW22 GeitzGSSW22 | Solving the Extended Job Shop Scheduling Problem with AGVs - Classical and Quantum Approaches | firstCS QUBO | y | | n | - | JSSP | |
| LiFJZLL22 LiFJZLL22 | Constraint Programming for a Novel Integrated Optimization of Blocking Job Shop Scheduling and Variable-Speed Transfer Robot Assignment | OPL CP Opt | ref | | n | - | BJSSP | endBeforeStart alternative noOverlap cumulative minCumulative alternative span |
| OuelletQ22 OuelletQ22 | A MinCumulative Resource Constraint | CP Coco | y | | y | - | | |
| OujanaAYB22 janaAYB22 | Solving a realistic hybrid and flexible flow shop scheduling problem through constraint programming: industrial case | CP Opt | n | | n | - | HFFS | alternative span |



Literature Survey - Application Areas

Table 8: Papers by Domain and Keyword

| Domain | Keyword | High | Medium | Low |
|------------------|-------------------|--|---|---|
| ApplicationAreas | crew scheduling | PourDERB18[308] | Mason01[259], Touraivane95[366] | WangB23[391], HeinzNVH22[169], HachemiGR11[158], BeldiceanuCO2[42], Bartak02[33], Bartak02a[32] |
| ApplicationAreas | dairies | EscobetPQPRA19[110] | PrataAN23[312] | |
| ApplicationAreas | dairy | EscobetPQPRA19[110] | PrataAN23[312] | |
| ApplicationAreas | datacenter | HermenierDL11[174] | | GalleguillosKSB19[124], Madi-WambaLOBM17[252], IfrimOS12[185], LetortBC12[228] |
| ApplicationAreas | datacentre | | | |
| ApplicationAreas | day ahead market | | | |
| ApplicationAreas | deep space | | | |
| ApplicationAreas | earth observation | SquillaciPR23[346], VerfaillieL01[375] | BensanaLV99[51] | PraletLJ15[311], SimoninAHL15[342], KelarevaTK13[197], OddiPCC03[288], SquillaciPR23[346] |
| ApplicationAreas | earth orbit | | | |
| ApplicationAreas | electroplating | | RodosekW98[320] | EfthymiouY23[106], WallaceY20[389], NovasH12[286] |
| ApplicationAreas | energy price | GrimesIOS14[152], IfrimOS12[185] | | PrataAN23[312], EscobetPQPRA19[110], BenediktSMVH18[49], HeoGLW18[161], LimHTB16[234], WinterMMW22[396], Astrand0F21[20] |
| ApplicationAreas | farming | | | Astrand0F21[20] |
| ApplicationAreas | forestry | HachemiGR11[158] | | AstrandJZ18[21], BonfiettiLBM12[62], LombardiBMB11[242], KorbaaYG99[206], PapaB98[296] |
| ApplicationAreas | hoist | EfthymiouY23[106], WallaceY20[389], RodosekW98[320] | NovasH12[286], BonfiettiLBM11[61] | |
| ApplicationAreas | medical | ShinBBHO18[338], WangMD15[392], TopalogluO11[364] | HechingH16[163], DejemeppeD14[93], RendIPHR12[318] | AkramNHRSA23[7], IsikYA23[186], AbreuN22[89], GeibingerKMMW21[133], FrimodigS19[121], Novas19[284], abs-1902-01193[8], GedikKEK18[132], BoothNB16[65], DoulabiRP14[103], Simonis07[344] |
| ApplicationAreas | nurse | GurPAE23[157], abs-1902-01193[8], ShinBBHO18[338], WangMD15[392], RendIPHR12[318], Simonis07[344], Mason01[259] | OuelletQ22[291], GeibingerKMMW21[133], GeibingerMM21[136], FrohnerTR19[122] | PerezGSL23[299], abs-2312-13682[300], FrimodigS19[121], NishikawaSTT18a[281], GedikKEK18[132], DoulabiRP14[103], TopalogluO11[364] |
| ApplicationAreas | offshore | | SubulanC22[347] | BoudreaultSLQ22[67] |
| ApplicationAreas | oven scheduling | LacknerMMWW23[224], LacknerMMWW21[223] | | |
| ApplicationAreas | patient | GurPAE23[157], FrimodigS19[121], ShinBBHO18[338], HechingH16[163], WangMD15[392], DejemeppeD14[93], RendIPHR12[318], TopalogluO11[364] | GeibingerKMMW21[133] | MurinR19[273], DoulabiRP14[103], Simonis07[344] |
| ApplicationAreas | perfect square | BeldiceanuCDP11[43], BeldiceanuCP08[44] | | |
| ApplicationAreas | physician | GeibingerKMMW21[133], ShinBBHO18[338] | | |
| ApplicationAreas | pipeline | LopesCSM10[246], MouraSCL08[271], MouraSCL08a[270], ErtIK91[109] | BeniniBGM06[50], WolinskiKG04[399] | GurPAE23[157], FrimodigS19[121], WangMD15[392], TopalogluO11[364], EfthymiouY23[106], PopovicCGNC22[307], HanenKP21[159], NishikawaSTT18[280], NishikawaSTT18a[281], LaborieRSV18[222], GilesH16[140], GoelSHFS15[144], SimoninAHL15[342], NovasH10[285], BarlattCG08[31], Wol03[397], KuchcinskiW03[218], GruianK98[155], Darby-DowmanLMZ97[86], SimonisC95[345] |
| ApplicationAreas | radiation therapy | FrimodigS19[121] | | |
| ApplicationAreas | railway | PourDERB18[308], CappartS17[73], Acuna-AgostMFG09[4], AronssonBK09[15], Geske05[139], MartinPY01[258] | LaborieRSV18[222], Mason01[259] | BogaerdW19[371], ZhouGL15[416], AtrihISB05[3], Wallace96[388] |
| ApplicationAreas | real time pricing | | HeoGLW18[161], GrimesIOS14[152] | LimHTB16[234] |
| ApplicationAreas | rectangle packing | YangSS19[402] | | MossigeGSMC17[269], VilimLS15[385], BeldiceanuCDP11[43], SchuttW10[334], BeldiceanuCP08[44] |

Literature Survey - Frequent Authors

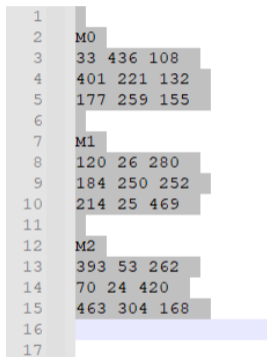
Table 5: Co-Authors of Articles/Papers

| Author | Entries |
|-----------------------|---|
| Andreas Schutt | YangSS19[402] KretzerSS17[217] YoungFS17[403] GoldwasserS17[146] SchuttS16[333] SzoreciS16[351] KretzerSS15[216] EvenSH15[111] EvenSH15a[112] SchuttFS13[330] cpaioir-SchuttFS13[329] GuSS13[156] SchuttCSW12[328] SchuttFSW11[332] SchuttW10[334] SchuttFSW09[331] |
| Nicolas Beldiceanu | Madi-WambaLOBM17[252] Madi-WambaB16[251] LetortCB15[230] LetortCB13[229] LetortBC12[228] ClercqPBJ11[81] BeldiceanuCDP11[43] BeldiceanuCP08[44] PoderB08[303] BeldiceanuP07[45] PoderB804[304] Beldiceanu02[42] AgounB92[5] |
| J. Christopher Beck | TangB20[352] BoothNB16[65] KoschB14[208] HeinsB13[168] HeinsKB13[165] HeinsB12[164] KovacsB11[210] BeckFW11[38] WatsonB08[303] KovacsB08[209] CarcareBFO5[74] WuBB05[401] BeckDF97[37] |
| Emmanuel Hebrard | JuvinaHHL23[188] AntunesHHEK21[111] GuelLHSH20[144] SimoninAHL15[342] SialaAH15[340] BessiereHMQW14[53] SimoninAHL12[341] BillautHL12[54] GrimesH11[150] GrimesH10[149] GrimesHM09[151] HebrardTW05[162] |
| Peter J. Stuckey | YangSS19[402] DomirovicS18[95] KretzerSS17[217] SchuttFS13[330] cpaioir-SchuttFS13[329] GuSS13[156] SchuttCSW12[328] SchuttFSW11[332] SchuttFSW09[331] |
| Michele Lombardi | BonfiettiZLM16[64] LombardiBM15[241] BartoliniBBLM14[35] BonfiettiLM14[63] LombardiM12[245] BonfiettiLBM12[62] BonfiettiLBM11[61] LombardiBMB11[242] LombardiM10[244] LombardiM09[243] HoweGSL07[373] |
| Pierre Lopez | JuvinaHHL23[188] JuvinaHL21[189] Polo-MejiaJLB20[306] NattaAL17[277] SimoninAHL15[342] NattaAL15[276] SimoninAHL12[341] BillautHL12[54] LahimerHL11[225] TrojtaHL11[367] LopezAKYG00[247] |
| Michela Milano | BonfiettiZLM16[64] LombardiBM15[241] BartoliniBBLM14[35] BonfiettiLM14[63] LombardiM12[245] BonfiettiLBM12[62] BonfiettiLBM11[61] LombardiBMB11[242] LombardiM10[244] LombardiM09[243] BeniniBGM06[50] |
| Petr Vilim | LaborieRSV16[222] VilimS15[385] Vilim11[382] Vilim09[380] cpaioir-Vilim09[381] VilimBC05[384] Vilim05[379] VilimBC04[383] Vilim04[378] Vilim03[377] Vilim02[376] |
| Christian Artigues | PoesdaAA23[309] PohLAK22[305] Polo-MejiaALB20[306] NattaAL17[277] SimoninAHL15[342] NattaAL15[276] SialaAH15[340] SimoninAHL12[341] ArtiguesBF04[16] ArtiguesR00[17] |
| John N. Hooker | Hooker17[181] HechingH16[163] CireCH13[80] CobanH10[82] Hooker06[180] Hooker05[178] cp-Hooker05[179] Hooker04[177] HookerY02[182] |
| Claude-Guy Quimper | BoudreauxSLQ22[67] OuelletQ22[991] Mercier-AubinGQ20[263] FahimOQ18[113] KameugneFGOQ18[192] OuelletQ18[290] GingsraQ16[141] BessiereHMQW14[53] OuelletQ13[289] |
| Pierre Schaus | CappartS17[73] CauwelaertDMS16[76] DejemeppeCS15[92] GayHLS15[128] GayHS15[129] cpaioir-GayHS15[130] HoundjiSWD14[183] GayS14[131] SchausHMCMD11[326] |
| Pascal Van Hentenryck | FontaineMH16[117] EvenSH15[111] EvenSH15a[112] SchausHMCMD11[326] MonetteDHO9[266] DoomsH08[102] HentenryckM08[173] HentenryckM04[172] DincbasSH00[101] |
| Philippe Baptiste | BaptisteB18[26] Baptiste09[25] BaptisteLPN06[27] ArtouchineB05[18] BaptisteP00[29] PapaB98[296] BaptisteP97[28] PapeB97[295] |
| Mats Carlsson | WessensCS20[394] MossesGC28[372] LetortCB15[230] LetortCB13[229] LetortBC12[228] BeldiceanuCDP11[43] BeldiceanuCP08[44] BeldiceanuC02[42] |
| Nyret Musliu | LacknerMMW23[224] WinterMMW22[396] LacknerMMW21[223] GelbingerKMMW21[133] GelbingerMM21[136] GelbingerMM19[135] abs-1911-04766[134] KletzanderM17[204] |
| Helmut Simonis | ArmstrongGOS22[14] ArmstrongGOS21[13] GrimesIOS14[152] IfrimOS12[185] Simonis07[344] SimonisC95[345] Simonis95[343] DincbasSH00[101] |
| Alessio Bonfietti | BonfiettiZLM16[64] BonfiettiLBM15[241] LombardiBM15[241] BonfiettiLM14[63] BonfiettiLBM12[62] BonfiettiLBM11[61] LombardiBMB11[242] |
| Zdenek Hansáček | Mehdizadeh-SomarijaniZ3[209] abs-2305-19888[179] HeinzNVZ2[169] VrhT121[387] BenediktMH20[48] BenediktSMVH18[49] KolbeH11[198] |
| Philippe Laborie | LumardILBR20[249] LaborieRSV18[222] LaborieLSA[221] MelgarejoSL15[6] VilimLS15[385] Laborie09[229] BaptisteLPN06[27] |
| Gabriela P. Henning | NovaraNH16[283] NovaraH14[287] NovaraH10[286] NovaraH10[285] ZebalioH10[409] ZebalioH05[408] QuirogaZH05[317] |
| Stefan Heinz | HeinsB13[168] HeinsKB13[165] HeinsSSW12[166] HeinsB12[164] HeinsS11[167] BertholdHLLMS10[52] |
| András Kovács | KovacsB11[210] KovacsK11[212] KovacsB08[209] KovacsV06[214] KovacsEKV05[211] KovacsV04[213] |
| Emmanuel Pöder | BeldiceanuCDP11[43] abs-0907-0939[302] BeldiceanuCP08[44] PoderB08[303] BeldiceanuP07[45] PoderBS04[304] |
| Mark Wallace | WallaceY20[389] HeGQMW18[181] SchuttFSW09[331] SakakouT00[325] RodloskW98[329] Wallace96[388] |
| Roman Barták | BartakS11[34] VilimBC05[384] VilimBC04[383] Bartak02[33] Bartak02a[32] |
| Yves Deville | HoundjiSWD14[183] DejemeppeD14[93] SchausHMCMD11[326] MonetteDHO9[266] MonetteDD07[265] |
| Thibaut Feydy | YoungFS17[403] SchuttFS13[330] cpaioir-SchuttFS13[329] SchuttFSW11[332] SchuttFSW09[331] |
| Roger Kameugne | KameugneFN23[193] KameugneFGOQ18[192] KameugneS15[191] KameugnePSN14[195] KameugnePSN11[194] |
| Claude Le Pape | BaptisteLPN06[27] BaptisteP00[29] PapaB98[296] BaptisteP97[28] PapeB97[295] |
| João M. Noronha | NovaraNH16[283] NovaraH14[287] NovaraH10[286] NovaraH10[285] |
| Louis-Martin Rousseau | DoulabRP16[104] PesantRR15[301] DoulabRP14[103] ChapadosR11[78] HachemiGR11[158] |
| André A. Cire | CireCH13[80] LopezCSM10[246] MouraSCL08[271] MouraSCL08a[270] |
| Luca Benini | BonfiettiLBM12[62] BonfiettiLBM11[61] LombardiBMB11[242] BeniniBGM06[50] |
| Cyrille Dejemeppe | CauwelaertDMS16[76] Dejemeppe16[91] DejemeppeCS15[92] DejemeppeD14[93] |
| Steven Gay | GayHLS15[128] GayHS15[129] cpaioir-GayHS15[130] GayHS14[131] |
| Tobias Gelbinger | GelbingerKMMW21[133] GelbingerMM21[136] GelbingerMM19[135] abs-1911-04766[134] |
| Diarmuid Grimes | GrimesIOS14[152] GrimesH11[150] GrimesH10[149] GrimesHM09[151] |
| Krzysztof Kuchcinski | WolinskiKG04[399] WolinskiKG04a[400] KuchcinskiW03[218] GruianK98[155] |
| Laurent Michel | TardivoDFMP23[354] SchausHMCMD11[326] HentenryckM08[173] HentenryckM04[172] |
| Florian Mischek | GelbingerKMMW21[133] GelbingerMM21[136] GelbingerMM19[135] abs-1911-04766[134] |

Most Recent Papers/Articles with Supplementary Materials

| Key | Size | Instances | MetaData | Format | Solutions | Checker |
|-----------------------|--------|-----------|----------|--------------|-----------|---------|
| AbreuN22 [10] | 1.3MB | 192 | n | TS | n | n |
| AntuoriHHEN21 [1] | 23.3MB | 120 | n | TS | n | n |
| ArmstrongGOS21 [4] | 11MB | 225 | n | dzn | n | n |
| BenderWS21 [5] | 116KB | 84 | y | TS | n | n |
| Bit-Monnot23 [6] | 23.5MB | 357 | n | TS | n | n |
| GeibingerKKMMW21 [15] | 40KB | 3 | - | dzn | n | n |
| GeibingerMM21 [16] | 13.9MB | 33 | n | xml | y | n |
| GeitzGSSW22 [17] | 16.0KB | 8 | y | json | n | n |
| IsikYA23 [26] | 3.9MB | 90 | n | xlsx | y | n |
| KimCMLLP23 [28] | 4.1MB | 4 | y | csv | n | n |
| KovacsTKSG21 [29] | 138MB | 18 | n | json json | n | n |

- Two stage open shop
- No buffer space
- Tasks of a job must follow each other without delay
- C_{\max} objective



AntuoriHHEN21 [1]

- Car manufacturing workshop
- Repetitive single vehicle pickup and delivery problem with time windows and capacity constraint
- Trolleys move components between two stages

```
1 492
2 8000
3
4 0 0 0 PF 1950 0 40 0 3625 2
5 1 0 0 DF 1950 1 40 0 3625 2
6 2 0 0 PE 1950 1 15 0 3625 2
7 3 0 0 DE 1950 0 15 0 3625 2
8 4 0 1 PF 1950 0 40 3625 7250 2
9 5 0 1 DF 1950 1 40 3625 7250 2
10 6 0 1 PE 1950 1 15 3625 7250 2
11 7 0 1 DE 1950 0 15 3625 7250 2
12 8 0 2 PF 1950 0 40 7250 10875 2
13 9 0 2 DF 1950 1 40 7250 10875 2
14 10 0 2 PE 1950 1 15 7250 10875 2
15 11 0 2 DE 1950 0 15 7250 10875 2
16 12 0 3 PF 1950 0 40 10875 14500 2
17 13 0 3 DF 1950 1 40 10875 14500 2
18 14 0 3 PE 1950 1 15 10875 14500 2
19 15 0 3 DE 1950 0 15 10875 14500 2
20 16 0 4 PF 1950 0 40 14500 18125 2
21 17 0 4 DF 1950 1 40 14500 18125 2
22 18 0 4 PE 1950 1 15 14500 18125 2
23 19 0 4 DE 1950 0 15 14500 18125 2
24 20 0 5 PF 1950 0 40 18125 21750 2
25 21 0 5 DF 1950 1 40 18125 21750 2
26 22 0 5 PE 1950 1 15 18125 21750 2
27 23 0 5 DE 1950 0 15 18125 21750 2
28 24 0 6 PF 1950 0 40 21750 25375 2
29 25 0 6 DF 1950 1 40 21750 25375 2
```


- Hybrid, flexible flowshop with transportation times between machines
- Instances in MiniZinc .dzn format
- Single file per instance
- Matches program in paper
- Integers, String, Arrays, Sets
- Tedious to parse for other solvers
- Could now be replaced by JSON
- Checker is easy to add

```
1 % J6J flowshop data
2 T = 1..154;
3 P = 1..134;
4 M = 1..80;
5 S = 1..8;
6 tuples = 1..800;
7 lb = 62;
8 ub = 63;
9 m = 80;
10 duration=
11 [3,10,4,4,6,8,7,4,1,4,7,10,1,4,9,9,9,3,1,1,6,8,6,8,2,3,6,6,8
12 ,5,9,4,3,3,7,10,5,10,8,3,10,9,2,6,6,4,7,7,9,4,10,8,8,5,9,4,3
13 capacity = [10,10,10,10,10,10,10];
14 stage =
15 [1,2,3,4,5,6,7,8,1,2,3,4,5,6,7,8,1,2,3,5,6,7,1,2,3,4,5,6,7,8
16 5,6,7,8,1,2,3,4,5,6,7,8,1,2,3,4,5,6,7,8,1,2,3,4,5,6,7,8,1,2,
17 machines =
18 [[1,2,3,4,5,6,7,8,9,10], [11,12,13,14,15,16,17,18,19,20], [21,
19 ,78,79,80], [1,2,3,4,5,6,7,8,9,10], [11,12,13,14,15,16,17,18,1
20 4,75,76,77,78,79,80], [1,2,3,4,5,6,7,8,9,10], [11,12,13,14,15,
21 14,15,16,17,18,19,20], [21,22,23,24,25,26,27,28,29,30], [31,32
22 [11,12,13,14,15,16,17,18,19,20], [21,22,23,24,25,26,27,28,29,
23 7,8,9,10], [11,12,13,14,15,16,17,18,19,20], [21,22,23,24,25,26
24 2,3,4,5,6,7,8,9,10], [11,12,13,14,15,16,17,18,19,20], [21,22,2
25 79,80], [1,2,3,4,5,6,7,8,9,10], [11,12,13,14,15,16,17,18,19,20
26 8,9,10], [11,12,13,14,15,16,17,18,19,20], [21,22,23,24,25,26,2
27 5,26,27,28,29,30], [31,32,33,34,35,36,37,38,39,40], [41,42,43,
28 22,23,24,25,26,27,28,29,30], [31,32,33,34,35,36,37,38,39,40],
29 9,20], [21,22,23,24,25,26,27,28,29,30], [41,42,43,44,45,46,47,
30 26,27,28,29,30], [31,32,33,34,35,36,37,38,39,40], [41,42,43,44
31 ,23,24,25,26,27,28,29,30], [31,32,33,34,35,36,37,38,39,40], [4
32 20], [21,22,23,24,25,26,27,28,29,30], [31,32,33,34,35,36,37,38
33 ,17,18,19,20], [21,22,23,24,25,26,27,28,29,30], [31,32,33,34,3
34 3,14,15,16,17,18,19,20], [21,22,23,24,25,26,27,28,29,30], [31,
35 ], [11,12,13,14,15,16,17,18,19,20], [21,22,23,24,25,26,27,28,2
36 6,7,8,9,10], [11,12,13,14,15,16,17,18,19,20], [21,22,23,24,25,
37 1,2,3,4,5,6,7,8,9,10], [11,12,13,14,15,16,17,18,19,20], [21,22
38 8,79,80]];
39
40 pexec =
41 [[1,2|2,3|3,4|4,5|5,6|6,7|7,8|9,10|10,11|11,12|12,13|13,14|1
42 9|49,50|50,51|51,52|52,53|53,54|55,56|56,57|57,58|58,59|59,6
43 4,95|95,96|96,97|97,98|99,100|100,101|101,102|102,103|103,10
44 |129,130|131,132|132,133|133,134|134,135|135,136|136,137|137
45 transportTime =
46 [[1,11,1|1,12,2|1,13,3|1,14,4|1,15,5|1,16,6|1,17,7|1,18,8|1,
47 4,114,15,2|4,16,3|4,17,4|4,18,5|4,19,6|4,20,7|5,11,5|5,12,4|
48 18,2|7,19,3|7,20,4|8,11,8|8,12,7|8,13,6|8,14,5|8,15,4|8,16,3
49 ,1|11,21,1|11,22,2|11,23,3|11,24,4|11,25,5|11,26,6|11,27,7|1
50 3,30,8|14,21,4|14,22,3|14,23,2|14,24,1|14,25,2|14,26,3|14,27
51 4|16,30,9|17,31,8|17,32,7|17,33,6|17,34,5|17,35,4|17,36,3|17,37,2|17,38,1]]
```

- Corn harvest scheduling
- Harvesters and transport vehicles
- Pre-emptive MRCPSP with fast-tracking, sequence-dependent setup times and synchronization of two resource types
- Meta-data: Describes format of data

| | |
|---|---|
| 1 | 4, 2, 4 |
| 2 | 64, 43 |
| 3 | 30, 30 |
| 4 | 0, 186.454, 228.75, 116.595, 175.71 |
| 5 | 3, 2, 2, 3, 2, 2, 2, 3 |
| 6 | 27.5399, 14.5452, 44.6473, 6.2793, 2.5734 |
| 7 | 35.4074, 25.5414, 44.8147, 10.3621, 22.0405 |
| 8 | |

- Disjunctive Scheduling
- Solver focused
- Open-/job-shop examples
- Mix of strings and numbers
- Text stream
- Different formats for job shop and open shop instances

```
1  nb_jobs nb_machines
2  10 10 0 0 0 0
3  Times
4  88 68 94 99 67 89 77 99 86 92
5  72 50 69 75 94 66 92 82 94 63
6  83 61 83 65 64 85 78 85 55 77
7  94 68 61 99 54 75 66 76 63 67
8  69 88 82 95 99 67 95 68 67 86
9  99 81 64 66 80 80 69 62 79 88
10 50 86 97 96 95 97 66 99 52 71
11 98 73 82 51 71 94 85 62 95 79
12 94 71 81 85 66 90 76 58 93 97
13 50 59 82 67 56 96 58 81 59 96
14  Machines
15  5 9 7 6 2 3 10 8 1 4
16  6 4 7 5 3 9 1 2 8 10
17  10 9 1 2 7 6 8 5 3 4
18  8 3 2 5 4 7 6 1 10 9
19  4 5 10 9 1 3 7 6 8 2
20  2 5 6 7 9 3 8 10 4 1
21  8 2 5 4 1 9 3 6 7 10
22  5 7 4 3 2 6 8 1 9 10
23  1 7 4 8 2 3 5 6 9 10
24  4 1 2 9 8 10 7 5 6 3
25
```

- Test lab Scheduling
- Real-world problem
- Extension of RCPSP
- Multiple files per instances
- XML format throughout

```
1 <?xml version="1.0" encoding="UTF-8"?>
2 <LabProjects>
3   <Project code="1">
4     <Name>Project 1</Name>
5     <Priority>1</Priority>
6     <CabinSafety>0.0</CabinSafety>
7     <Tasks>
8       <Task id="1">
9         <Name>Task 1.1</Name>
10        <Duration>9.747909850747426</Duration>
11        <ReleaseDate>0</ReleaseDate>
12        <DueDate>58</DueDate>
13        <Deadline>65</Deadline>
14        <WorkbenchRequired>false</WorkbenchRequired>
15        <TaskModes>1 2</TaskModes>
16        <AvailableWorkbenches></AvailableWorkbenches>
17        <QualifiedEmployees>1 3 7</QualifiedEmployees>
18        <PreferredEmployees>1 3 7</PreferredEmployees>
19        <EquipmentRequirements>
20          <Group groupId="1">
21            <Demand>1</Demand>
22            <AvailableDevices>1 2</AvailableDevices>
23          </Group>
24        </EquipmentRequirements>
25      </Task>
26    </Tasks>
27    <LinkedTasks>
28      <LinkedSet>1</LinkedSet>
29    </LinkedTasks>
30    <TaskFamilies>
31      <Family name="FA" setup="1.7807819167841257">
32        <Tasks>1</Tasks>
33      </Family>
34      <Family name="FB" setup="2.9780123418384914"/>
35    </TaskFamilies>
36  </Project>
37  <Project code="2">
38    <Name>Project 2</Name>
39    <Priority>1</Priority>
40    <CabinSafety>0.0</CabinSafety>
41    <Tasks/>
```

- Extension of Hybrid Flow-shop (no-wait, blocking, sequence dependent setup)
- Uses Excel .xlsx format for input and output
- Understandable as format of result summaries
- Horrible choice as data input format
 - Automatic type conversions by Excel
 - Hard to retrieve input data in original form

| | | | | | | | | | | | | | | | |
|-----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| 165 | 8 | 3 | 25 | 20 | 2 | 15 | 11 | 45 | 0 | 31 | 23 | 42 | 2 | 34 | 41 |
| 166 | 9 | 50 | 46 | 27 | 12 | 23 | 9 | 3 | 27 | 0 | 49 | 32 | 50 | 42 | 19 |
| 167 | 10 | 27 | 13 | 22 | 36 | 39 | 27 | 15 | 43 | 32 | 0 | 31 | 35 | 49 | 25 |
| 168 | 11 | 43 | 27 | 12 | 18 | 20 | 36 | 48 | 39 | 39 | 10 | 0 | 44 | 38 | 39 |
| 169 | 12 | 45 | 13 | 2 | 36 | 12 | 1 | 39 | 33 | 45 | 24 | 27 | 0 | 30 | 11 |
| 170 | 13 | 35 | 42 | 2 | 30 | 20 | 10 | 3 | 47 | 34 | 45 | 4 | 35 | 0 | 8 |
| 171 | 14 | 26 | 27 | 14 | 6 | 10 | 37 | 2 | 35 | 11 | 28 | 28 | 43 | 11 | 0 |
| 172 | 15 | 23 | 18 | 35 | 33 | 23 | 50 | 47 | 12 | 10 | 13 | 4 | 12 | 11 | 49 |
| 173 | 16 | 20 | 13 | 17 | 37 | 31 | 10 | 19 | 36 | 21 | 14 | 38 | 7 | 50 | 28 |
| 174 | 17 | 2 | 9 | 38 | 44 | 12 | 12 | 1 | 12 | 39 | 29 | 2 | 3 | 26 | 34 |
| 175 | 18 | 11 | 30 | 40 | 2 | 44 | 17 | 26 | 28 | 40 | 40 | 48 | 32 | 12 | 34 |
| 176 | 19 | 5 | 41 | 3 | 8 | 37 | 7 | 48 | 19 | 30 | 2 | 19 | 4 | 20 | 31 |
| 177 | 20 | 40 | 43 | 1 | 27 | 16 | 17 | 47 | 32 | 9 | 37 | 50 | 39 | 11 | 4 |
| 178 | | | | | | | | | | | | | | | |
| 179 | | | 1 | 1 | 1 | 0 | 1 | 1 | 1 | | | | | | |
| 180 | | | 1 | 0 | 1 | 1 | 0 | 0 | 1 | | | | | | |
| 181 | | | 1 | 0 | 1 | 1 | 1 | 1 | 0 | | | | | | |
| 182 | | | 1 | 0 | 1 | 0 | 1 | 1 | 1 | | | | | | |
| 183 | | | 1 | 1 | 1 | 1 | 0 | 1 | 1 | | | | | | |
| 184 | | | 1 | 1 | 1 | 1 | 1 | 1 | 1 | | | | | | |
| 185 | | | 1 | 1 | 1 | 0 | 0 | 1 | 0 | | | | | | |
| 186 | | | 1 | 0 | 0 | 1 | 1 | 1 | 1 | | | | | | |
| 187 | | | 1 | 1 | 1 | 0 | 1 | 1 | 1 | | | | | | |
| 188 | | | 1 | 1 | 0 | 1 | 0 | 1 | 1 | | | | | | |
| 189 | | | 1 | 1 | 1 | 0 | 1 | 1 | 1 | | | | | | |
| 190 | | | 0 | 1 | 1 | 1 | 1 | 1 | 1 | | | | | | |
| ... | | | . | . | . | . | . | . | . | | | | | | |

- Real-world work-load balancing problem
- Made-to-order printing machines
- Nice JSON format of data
- Real-life data
- One instance per file, one file per instance
- Task length given as float
- Machine capacity given as float

```
1 {
2   "info": {
3     "days": 14,
4     "objective": {
5       "penaltyPerDay": 1,
6       "oneTimePenalty": 3,
7       "jobWeight": 1,
8       "projects": []
9     }
10  },
11  "tasks": [
12    {
13      "id": 835789,
14      "machine": 846644,
15      "job": 972494,
16      "length": 46.085566752371655,
17      "earliest_start": 0,
18      "directly_after_last": false,
19      "free_days_before": 0
20    },
21    {
22      "id": 708746,
23      "machine": 521987,
24      "job": 972494,
25      "length": 22.595964864783412,
26      "earliest_start": 1,
27      "directly_after_last": false,
28      "free_days_before": 0
29    },
30    {
31      "id": 578563,
32      "machine": 908456,
33      "job": 972494,
34      "length": 0.09596492713072255,
35      "earliest_start": 2,
36      "directly_after_last": false,
37      "free_days_before": 0
38    },
39    {
40      "id": 472983,
41      "machine": 224663,
```

Challenges

- Data formats are often ad-hoc, token streams common
- Meaning of value depends on position in stream
- Solutions very rarely provided
 - If given, only one (best) solution is given
 - Sometimes can be generated from code which is provided
- Checkers non-existent
- For many papers, extracting the constraint model is not the challenge
 - Finding a good solution quickly enough is

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Literature Survey

Papers with Data and (Solutions or Programs)

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ROADEF2022

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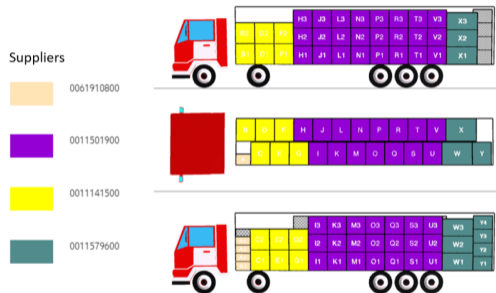
Bibliography

Realistic Examples

- Two examples of a more complex nature
- Realistic, but not real problem set
- Show complexity of real-world problems

Roadef2022 Challenge

- Competition by French OR society Roadef, European OR society Euro
- Problem provided by Renault
- Schedule transport of components from suppliers to factories
- Decide when to transport item, how to pack them into trucks
- Decide how many resources (trucks) are needed
- Not a vehicle routing problem (routes predefined and given)
- Objective Minimize cost (resources plus earliness cost of items)



Potential Trucks

| | Supplier code;Supplier loading order;Supplier dock;Supplier dock loading order;Plant code;Plant dock;Plant dock loading order;Product code;Arrival time;Id |
|----|---|
| 1 | truck;Length;Width;Height;Max weight;Stack with multiple docks;Max density;Max weight on the bottom item in stacks;Cost;EMmm;EMm;CM;CJfm;CJfc;CJfh;EM;EJhr;EJcr;EJeh |
| 2 | 0062069400;1;;1;0090018000;X0;1;852480062R;202208182025;P230711301;14500;2400;2800;30000;0;1500;100000;1500;12000;31500;7808,000;3800;1040;3330;7300,000;7630;2350;1670 |
| 3 | 0062069400;1;;1;0090018000;X0;1;745322815R;202208182025;P230711301;14500;2400;2800;30000;0;1500;100000;1500;12000;31500;7808,000;3800;1040;3330;7300,000;7630;2350;1670 |
| 4 | 0062069400;1;;1;0090018000;X0;1;8201677103;202208182025;P230711301;14500;2400;2800;30000;0;1500;100000;1500;12000;31500;7808,000;3800;1040;3330;7300,000;7630;2350;1670 |
| 5 | 0062069400;1;;1;0090018000;X0;1;781419006R;202208182025;P230711301;14500;2400;2800;30000;0;1500;100000;1500;12000;31500;7808,000;3800;1040;3330;7300,000;7630;2350;1670 |
| 6 | 0062069400;1;;1;0090018000;X0;1;781405634R;202208182025;P230711301;14500;2400;2800;30000;0;1500;100000;1500;12000;31500;7808,000;3800;1040;3330;7300,000;7630;2350;1670 |
| 7 | 0062069400;1;;1;0090018000;X0;1;821474009R;202208182025;P230711301;14500;2400;2800;30000;0;1500;100000;1500;12000;31500;7808,000;3800;1040;3330;7300,000;7630;2350;1670 |
| 8 | 0062069400;1;;1;0090018000;X0;1;766361764R;202208182025;P230711301;14500;2400;2800;30000;0;1500;100000;1500;12000;31500;7808,000;3800;1040;3330;7300,000;7630;2350;1670 |
| 9 | 0062069400;1;;1;0090018000;X0;1;791407225R;202208182025;P230711301;14500;2400;2800;30000;0;1500;100000;1500;12000;31500;7808,000;3800;1040;3330;7300,000;7630;2350;1670 |
| 10 | 0062069400;1;;1;0090018000;X0;1;776514302R;202208182025;P230711301;14500;2400;2800;30000;0;1500;100000;1500;12000;31500;7808,000;3800;1040;3330;7300,000;7630;2350;1670 |
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| 12 | 0062069400;1;;1;0090018000;X0;1;781400316R;202208182025;P230711301;14500;2400;2800;30000;0;1500;100000;1500;12000;31500;7808,000;3800;1040;3330;7300,000;7630;2350;1670 |
| 13 | 0062069400;1;;1;0090018000;X0;1;625191617R;202208182025;P230711301;14500;2400;2800;30000;0;1500;100000;1500;12000;31500;7808,000;3800;1040;3330;7300,000;7630;2350;1670 |
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| 16 | 0062069400;1;;1;0090018000;X0;1;764124757R;202208182025;P230711301;14500;2400;2800;30000;0;1500;100000;1500;12000;31500;7808,000;3800;1040;3330;7300,000;7630;2350;1670 |
| 17 | 0062069400;1;;1;0090018000;X0;1;781413811R;202208182025;P230711301;14500;2400;2800;30000;0;1500;100000;1500;12000;31500;7808,000;3800;1040;3330;7300,000;7630;2350;1670 |
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| 20 | 0062069400;1;;1;0090018000;X0;1;763571615R;202208182025;P230711301;14500;2400;2800;30000;0;1500;100000;1500;12000;31500;7808,000;3800;1040;3330;7300,000;7630;2350;1670 |
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| 27 | 0062069400;1;;1;0090018000;X0;1;8201745175;202208182025;P230711301;14500;2400;2800;30000;0;1500;100000;1500;12000;31500;7808,000;3800;1040;3330;7300,000;7630;2350;1670 |
| 28 | 0062069400;1;;1;0090018000;X0;1;762428480R;202208182025;P230711301;14500;2400;2800;30000;0;1500;100000;1500;12000;31500;7808,000;3800;1040;3330;7300,000;7630;2350;1670 |
| 29 | 0062069400;1;;1;0090018000;X0;1;762432908R;202208182025;P230711301;14500;2400;2800;30000;0;1500;100000;1500;12000;31500;7808,000;3800;1040;3330;7300,000;7630;2350;1670 |

Observations

- Data size varies between instances, but is typically (very) large
- Four stages of data availability, 150 instances in total
- One sample solution given
- But: Checker (in java) provided, normative
- Problem description 11+8 pages
- Data tables not normalized, contains much redundant information
- Normalizing data leads to UML Object Model on next slide

Defined Output Format

- Three files
 - Trucks used
 - Stacks built
 - Pieces placed
- No direct link between planned and scheduled trucks
- Concept of stack is redundant
- One item results in multiple pieces
- Link between trucks, stacks, pieces and input data by string ids

| | | | |
|---|-------|------------|---|
| Id truck | char | P380411201 | |
| Loaded length | int | 12500 mm | $max_{s \in \mathcal{F} \cup \mathcal{S}_t} sx_s^e$ |
| Weight of loaded items | float | 1894,31 | kg |
| Volume of loaded items | float | 14,544 | m^3 |
| Weight on the middle axle of the trailer (em^m) | float | 1875,83 | kg |
| Weight on the rear axle of the trailer (em^r) | float | 18,47 | kg |

| Field | Type | Example | Comments |
|--------------------------|------|--------------|---|
| Id truck | char | P380411201 | Must be defined in the output trucks file |
| Id stack | char | P380411201_1 | |
| Stack code | char | A | To be used for display (cf FIGURE 1) |
| X origin (sx_s^o) | int | 0 | mm |
| Y origin (sy_s^o) | int | 0 | mm |
| Z origin (sz_s^o) | int | 0 | mm |
| X extremity (sx_s^e) | int | 1010 | mm |
| Y extremity (sy_s^e) | int | 1206 | mm |
| Z extremity (sz_s^e) | int | 407 | mm |

| Field | Type | Example | Comments |
|-------------|------|------------------------|---|
| Item ident | char | 00900160_20221201_2314 | Must be defined in the input items file |
| Id truck | char | P380411201 | Must be defined in the output trucks file |
| Id stack | char | P380411201_1 | Must be defined in the output stacks file |
| Item code | char | A1 | To be used for display (cf FIGURE 1) |
| X origin | int | 0 | mm |
| Y origin | int | 0 | mm |
| Z origin | int | 0 | mm |
| X extremity | int | 1010 | mm |
| Y extremity | int | 1206 | mm |
| Z extremity | int | 407 | mm |

Complex Side Constraints

- Some of the constraints are not just simple, linear formulas

$$ej^e = \frac{\sum_{s \in \overline{TS}_t} (sx_s^o + \frac{(sx_s^e - sx_s^o)}{2}) \times sm_s}{tm_t}$$

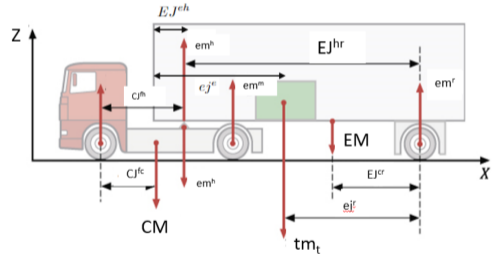
$$ej^r = EJ^{eh} + EJ^{hr} - ej^e$$

$$em^h = \frac{tm_t \times ej^r + EM \times EJ^{er}}{EJ^{hr}}$$

$$em^r = tm_t + EM - em^h$$

$$em^m = \frac{CM \times CJ^{fc} + em^h \times CJ^{fh}}{CJ^{fm}}$$

- Interpretation requires detailed physical model



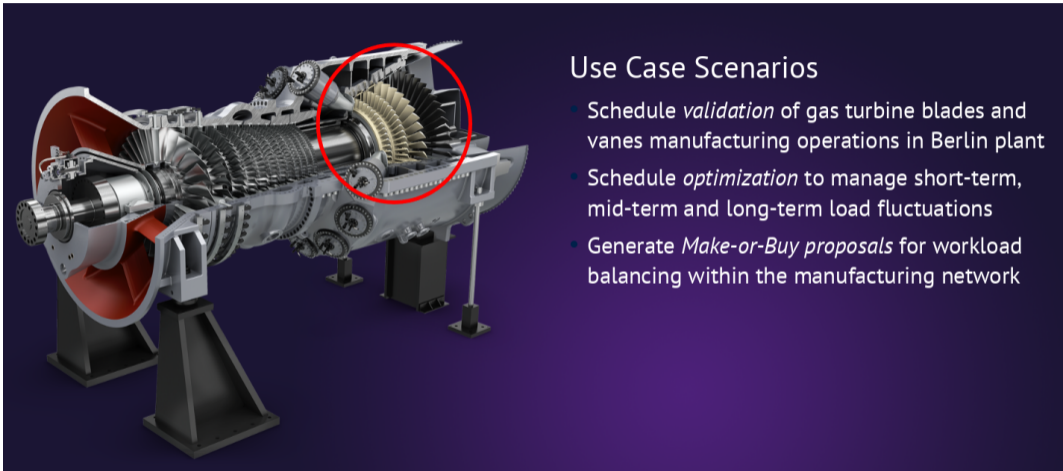
A Grand Challenge for Constraint Acquisition

- Can you extract a transferable model of this problem?
 - Given the data and solutions of all problem instances
- Not too hard to find packing constraints for pieces
- Packing constraints for stacks are simple
- Real problem
 - How many stacks are needed?
 - How many trucks are needed?
 - Many non-trivial side constraints!
- Previous competitions provide similar challenges
 - There is a checker!
 - Lots of instances
 - Solutions not known until challenge end

An Industrial Example

- ASSISTANT Siemens Energy use case
- Mid/Long-term scheduling/production planning
- Realistic/not real data
- Rather complex constraint model
 - Multi-stage BOM
 - Alternative Process Paths
 - Alternative machines
 - Quality/cost based routing preferences
 - Potential outsourcing of certain steps
 - Machine specific calendars
 - Infeasible release/due date pairs
 - Calendar dependent speed reduction
 - Complex manpower constraints

Assistant Siemens Energy Use Case



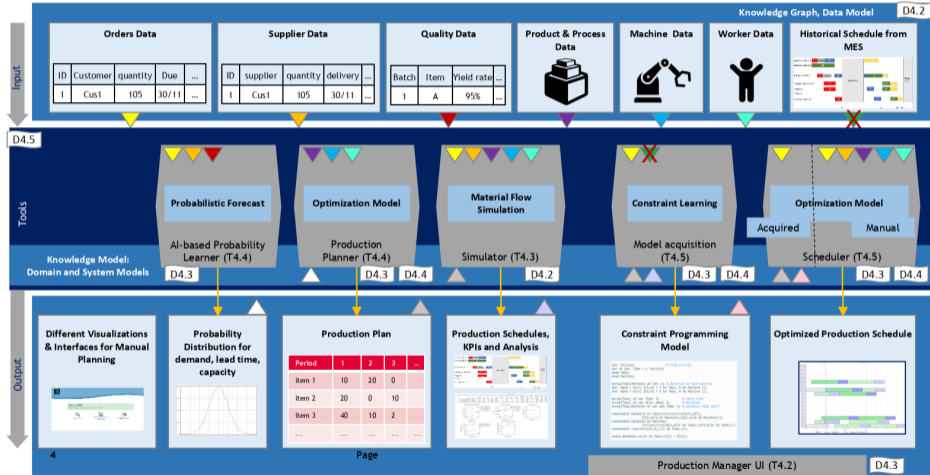
Use Case Scenarios

- Schedule *validation* of gas turbine blades and vanes manufacturing operations in Berlin plant
- Schedule *optimization* to manage short-term, mid-term and long-term load fluctuations
- Generate *Make-or-Buy proposals* for workload balancing within the manufacturing network

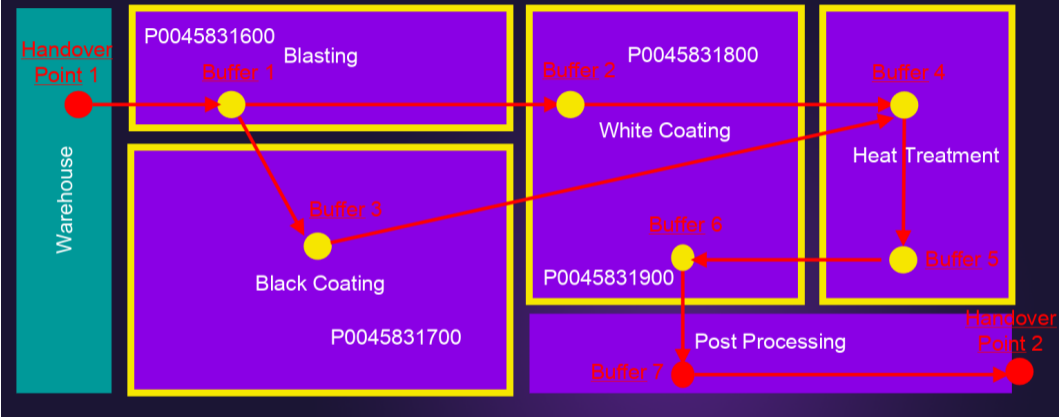
Digital Twin

Intelligent digital twin for process planning and scheduling

ASSISTANT



SE Product Routing



Full Scale Datasets

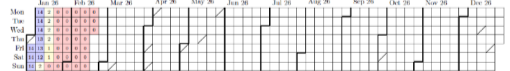
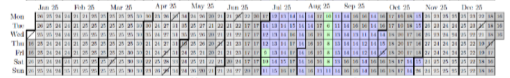
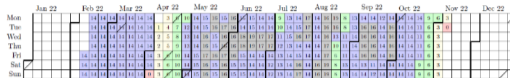
Berlin06: 96 orders, 9 months horizon, previous review



Berlin07: 450 orders, 4 years horizon

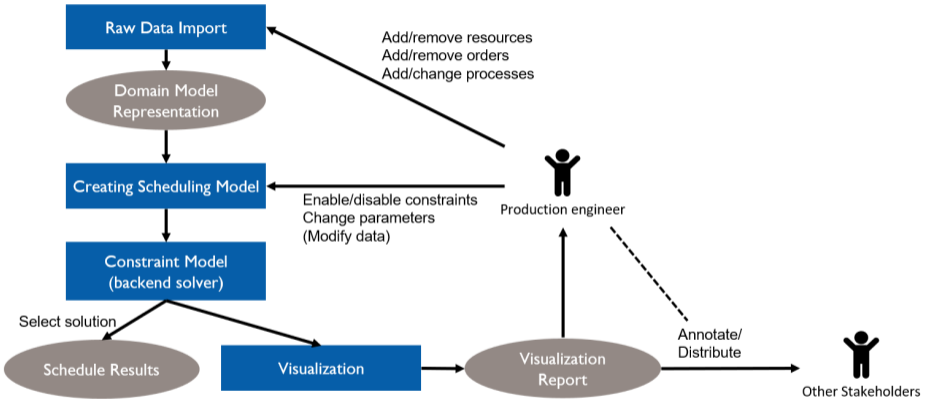
Berlin08: 559 orders, Christmas gap added

Berlin08a: 670 orders, filling gaps



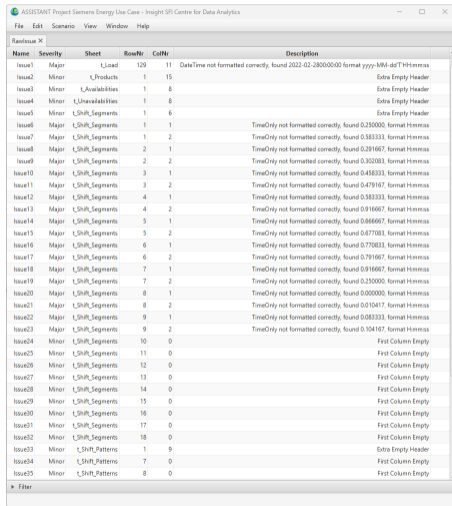
Value in cell indicates active orders
Yellow and red colors indicate low order volume

Optimizer High Level Structure



Raw Data - Manual Data Entry Causes Problems

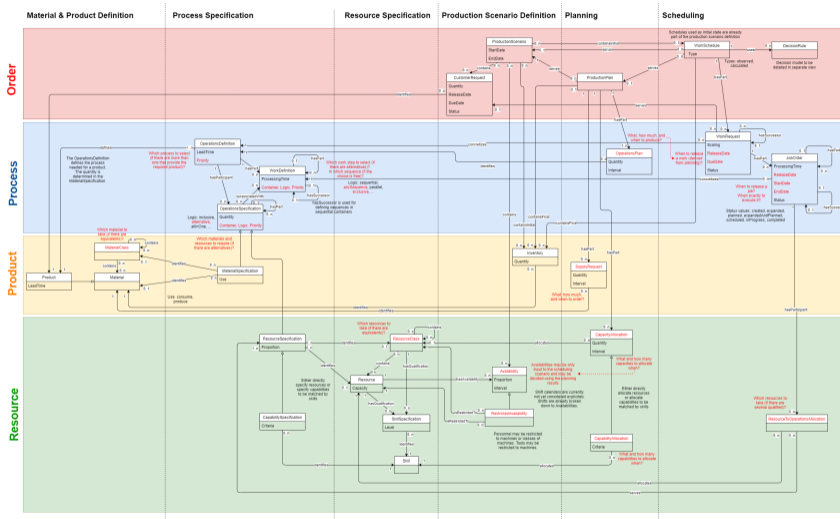
- Raw data come from spreadsheet
 - 20 tabs
- Excel is a particularly bad input data format
- Realistic, not real data
- Created by hand/automatically from existing test scenarios
- Series of files Berlin01 - Berlin05 were too inconsistent to run
- Berlin06 still contains some errors
- Optimizer explains all issues that it finds



The screenshot shows a software interface with a table of issues. The table has columns for Name, Severity, Sheet, RowNr, ColNr, and Description. The issues listed are:

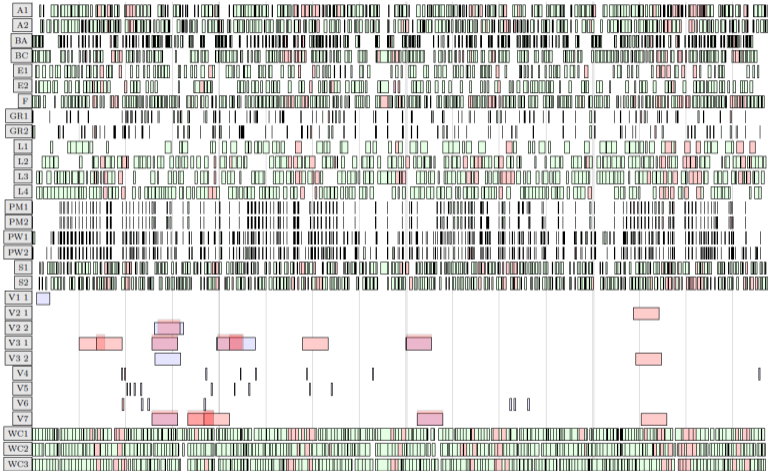
| Name | Severity | Sheet | RowNr | ColNr | Description |
|---------|----------|--------------------|-------|-------|--|
| Issue1 | Major | t_Load | 129 | 11 | DateTime not formatted correctly, found 2022-02-280000:00 format yyyy-MM-ddTHH:mm:ss |
| Issue2 | Minor | t_Products | 1 | 15 | Extra Empty Header |
| Issue3 | Minor | t_Availability | 1 | 8 | Extra Empty Header |
| Issue4 | Minor | t_Unavailabilities | 1 | 8 | Extra Empty Header |
| Issue5 | Minor | t_Shift_Segments | 1 | 6 | Extra Empty Header |
| Issue6 | Major | t_Shift_Segments | 1 | 1 | TimeOnly not formatted correctly, found 0.250000, format H:mm:ss |
| Issue7 | Major | t_Shift_Segments | 1 | 2 | TimeOnly not formatted correctly, found 0.583333, format H:mm:ss |
| Issue8 | Major | t_Shift_Segments | 2 | 1 | TimeOnly not formatted correctly, found 0.291667, format H:mm:ss |
| Issue9 | Major | t_Shift_Segments | 2 | 2 | TimeOnly not formatted correctly, found 0.302083, format H:mm:ss |
| Issue10 | Major | t_Shift_Segments | 3 | 1 | TimeOnly not formatted correctly, found 0.458333, format H:mm:ss |
| Issue11 | Major | t_Shift_Segments | 3 | 2 | TimeOnly not formatted correctly, found 0.479167, format H:mm:ss |
| Issue12 | Major | t_Shift_Segments | 4 | 1 | TimeOnly not formatted correctly, found 0.583333, format H:mm:ss |
| Issue13 | Major | t_Shift_Segments | 4 | 2 | TimeOnly not formatted correctly, found 0.916667, format H:mm:ss |
| Issue14 | Major | t_Shift_Segments | 5 | 1 | TimeOnly not formatted correctly, found 0.666667, format H:mm:ss |
| Issue15 | Major | t_Shift_Segments | 5 | 2 | TimeOnly not formatted correctly, found 0.677083, format H:mm:ss |
| Issue16 | Major | t_Shift_Segments | 6 | 1 | TimeOnly not formatted correctly, found 0.770833, format H:mm:ss |
| Issue17 | Major | t_Shift_Segments | 6 | 2 | TimeOnly not formatted correctly, found 0.791667, format H:mm:ss |
| Issue18 | Major | t_Shift_Segments | 7 | 1 | TimeOnly not formatted correctly, found 0.916667, format H:mm:ss |
| Issue19 | Major | t_Shift_Segments | 7 | 2 | TimeOnly not formatted correctly, found 0.250000, format H:mm:ss |
| Issue20 | Major | t_Shift_Segments | 8 | 1 | TimeOnly not formatted correctly, found 0.000000, format H:mm:ss |
| Issue21 | Major | t_Shift_Segments | 8 | 2 | TimeOnly not formatted correctly, found 0.010417, format H:mm:ss |
| Issue22 | Major | t_Shift_Segments | 9 | 1 | TimeOnly not formatted correctly, found 0.083333, format H:mm:ss |
| Issue23 | Major | t_Shift_Segments | 9 | 2 | TimeOnly not formatted correctly, found 0.104167, format H:mm:ss |
| Issue24 | Minor | t_Shift_Segments | 10 | 0 | First Column Empty |
| Issue25 | Minor | t_Shift_Segments | 11 | 0 | First Column Empty |
| Issue26 | Minor | t_Shift_Segments | 12 | 0 | First Column Empty |
| Issue27 | Minor | t_Shift_Segments | 13 | 0 | First Column Empty |
| Issue28 | Minor | t_Shift_Segments | 14 | 0 | First Column Empty |
| Issue29 | Minor | t_Shift_Segments | 15 | 0 | First Column Empty |
| Issue30 | Minor | t_Shift_Segments | 16 | 0 | First Column Empty |
| Issue31 | Minor | t_Shift_Segments | 17 | 0 | First Column Empty |
| Issue32 | Minor | t_Shift_Segments | 18 | 0 | First Column Empty |
| Issue33 | Minor | t_Shift_Patterns | 1 | 9 | Extra Empty Header |
| Issue34 | Minor | t_Shift_Patterns | 7 | 0 | First Column Empty |
| Issue35 | Minor | t_Shift_Patterns | 8 | 0 | First Column Empty |

Domain Model - Knowledge Graph



Single Solution for Berlin 08a - Shows Only 20% of Tasks in Model

Overall End 14/1/2026 06:37



Thu 10/2/2022

Fri 10/2/2023

Sat 10/2/2024

Sun 9/2/2025

Internal External Late Adjusted

Challenges for CA

- Input data not fully consistent
- Decide what to do with detected problems
- Solution only shows active part of schedule
- Large set of optional tasks not visible as not active
- Input data contain many fields which are irrelevant for scheduler
 - Component level information
 - Nomenclature
- Many task properties are computed from input data
 - Understand links between multiple objects
 - Time resolution/rounding

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Summary

- Presented different sources for CA benchmarks from simple to complex
- Few sources present all elements required for CA
- Benchmarks rather than competition
- Why data format is important
- As authors, please provide data, solutions, checkers
- Algorithms are necessary, but not sufficient for Constraint Acquisition

Ad: ACP Winter School 2024

- March 25-29, Aussois, France, <https://school.a4cp.org/winter2024/>

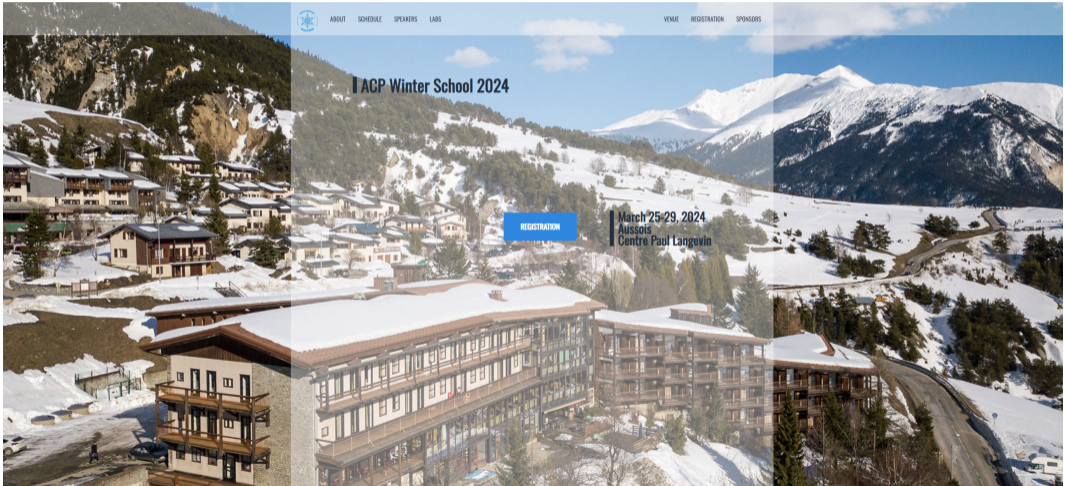


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